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## 

- Goal: Compare funding alternatives over time
- Components:
- Nomenclature \& Definitions
- Fundamental Equations
- Cost Concepts
- Interest Tables
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-Vocabulary
- P: Present Value
- F: Future Value
- i: Interest compounded each period
- n: Number of compounding periods
- m: Number of compounding periods per year
- Standard notation: (F|P,i,n)
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## 

## - Simple

- Interest paid out as earned


## - Compound

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- Interest increased incrementally over time
- 3 ways to represent, not always straight forward $\qquad$
- Actual (i): rate associated with compounding period (use for calcs)
- Nominal (r): annual rate w/o effects of compounding
- Effective ( $i_{e}$ ): effect of actual interest rate over a different period

$$
\mathrm{i}=\mathrm{r} / \mathrm{m} \quad \mathrm{i}_{\mathrm{e}}=(1+\mathrm{i})^{\mathrm{m}}-1
$$

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- Horizontal timeline
- Vertical cash-flow lines, direction depends on POV

- Single Payments
- Convert lump sums between present (P) and future (F) worth
- Uniform Series
- Convert equal payments (A) to present (P) or future (F) worth
- Arithmetic Gradient
- Convert periodic payments of increasing/decreasing amount (G) to present (P) worth


## - Composite Flows

- Convert combinations of these payments (P/F/A/G) to present (P) or future (F) worth


## 

- Tables save us from repeating the same calculations $\qquad$
- Steps:
- Draw cash flow diagram
- Identify what you are given and what you want to find
- Select the correct relationship/equation
- Fill out the symbolic notation
- Match notation values to the interest factor tables $\qquad$
- Pick correct value!
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## 

- The cash flow diagram you draw for the problem MUST match the fundamental cash flow diagram perfectly in order to use its equation
- If it doesn't, you need to make it fit!
- Brute force
- Treat all payments at P/F and convert to what you are looking for
- Breakup
- Separate payments into types and convert
- Look for patterns- much faster!!


## 

- Convert everything to a set timeframe
- Net present worth
- Convert all cash flows to an equivalent value at a time designated as the present $(\mathrm{t}=0$ )
- Net annual worth
- Convert all cash flows to an equivalent uniform series spanning the time period: $\mathrm{t}=1$ through $\mathrm{t}=\mathrm{n}$
- Inverse sign of equivalent annual cost


## 

- Ratio of NPW of benefits to NPW of costs $\qquad$
- Benefits may also include "disbenefits" (negative impacts)
- Compare two alternatives, or one alternative to the do-nothing alternative
- When $B C R>1$ (or $\Sigma B-\Sigma C>0$ ), accept the alternative



## 

- Don't be intimidated by the equations
- You can solve most problems by finding the right equation $\qquad$
- Pay attention to units
- Do as many practice problems as you can!
- Get to know the FE reference handbook.
- Download a copy at: http://www.ncees.org/Exams/Study_materials/ Download_FE_Supplied-Reference_Handbook.php
- When in doubt, work backwards!
- Plug answers into the equations and see what works

